

NO CALCULATOR

Given $P(x)$, rewrite in Vertex form, Identity the Vertex, X and Y intercepts, Domain and Range and sketch the graph.

Name _____ *Key* Per. _____

$$1. P(x) = -2(x+1)^2 + 6$$

$$3 = (x+1)^2 \quad 2. P(x) = 3x^2 - 18x + 25$$

$$3. P(x) = 2x^2 + 4x - 3$$

$$V: (-1, 6) \downarrow$$

$$\pm\sqrt{3} = x+1$$

$$3(x^2 - 6x + 9) + 25 - 27$$

$$2(x^2 + 2x + 1) - 3 - 2$$

$$X = -1 \pm \sqrt{3}$$

$$y = 3(x-3)^2 - 2 \uparrow \frac{2}{3} = (x-3)^2$$

$$y = 2(x+1)^2 - 5$$

$$Y = 4$$

$$D: (-\infty, \infty) \quad R: [-\infty, 6]$$

$$V: (3, -2) \quad y = 25$$

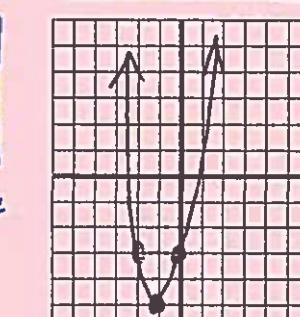
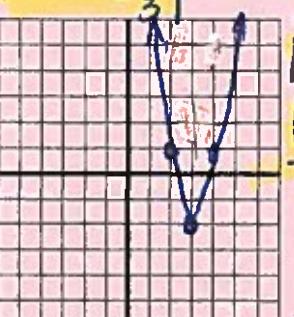
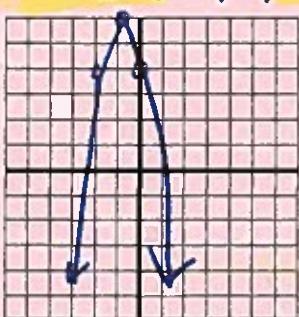
$$V: (-1, -5)$$

$$Y = 4$$

$$D: (-\infty, \infty) \quad R: [-\infty, 6]$$

$$X = 3 \pm \frac{\sqrt{16}}{3}$$

$$X = -1 \pm \frac{\sqrt{10}}{2}$$



4. If a ball is thrown upward with a velocity of 64 ft/s, its height (in feet) after t seconds is given by $y = 64t - 16t^2$. What is the maximum height attained by the ball? When does the ball reach its maximum height?

$$y = -16t^2 + 64t$$

$$y = -16(t^2 - 4t + 4) + 64$$

$$y = -16(t-2)^2 + 64$$

$$V: (2, 64)$$

$$\text{Max } @ 64$$

after 2 seconds

5. Find the maximum or minimum point. (State whether it is a max or min) $P(x) = -2x^2 + 4x - 3$

$$\text{Optimal } X = \frac{-b}{2a} \rightarrow X = \frac{-4}{-4} = 1 \quad y = -2 + 4 - 3 = 1$$

$$\text{Max } @ 1$$

Graph the function using all intercepts making sure it exhibits the proper end behavior.

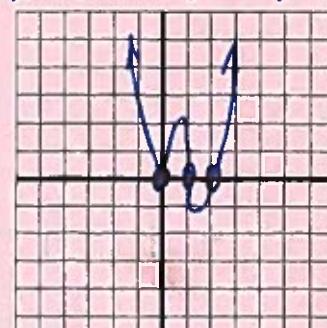
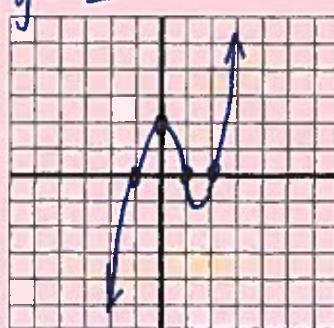
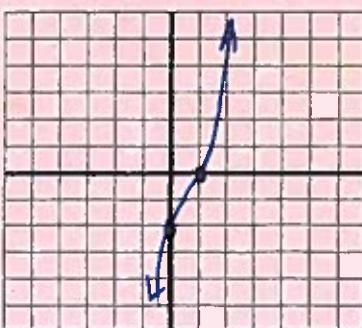
$$6. P(x) = 2(x-1)^3$$

$$7. P(x) = (x-1)(x+1)(x-2)$$

$$8. P(x) = x^4 - 3x^3 + 2x^2$$

$$\begin{aligned} \text{deg: 3} & \text{ LC: + } x=1 (3) \text{ bends} \\ \text{rt } \uparrow, \text{ left } \downarrow & \quad y_{\text{int}}: -2 \end{aligned}$$

$$\begin{aligned} \text{deg: 3} & \text{ LC: + } \\ \text{rt } \uparrow, \text{ left } \downarrow & \\ x = 1, -1, 2 & \\ y = 2 & \end{aligned}$$



$y = 0$
bounce @ 0

Determine the end behavior of $P(x)$.

9. $P(x) = -4x^4 + 5x^3 - 2x^2 + 10$

deg: 4 bc: -1 sort ↓ + left ↓ $x \rightarrow +\infty, y \rightarrow -\infty$
 $x \rightarrow -\infty, y \rightarrow -\infty$

CALCULATORS ALLOWED

Find the quotient and remainder using long division.

10. $\frac{x^6 + x^4 + x^2 + 1}{x^2 + 1}$

$$\boxed{X^4 + 1}$$

$$\begin{array}{r} X^4 + 1 \\ \hline X^2 + 0X + 1 \big) \overline{X^6 + 0X^5 + X^4 + 0X^3 + X^2 + 0X + 1} \\ \underline{- X^6 - 0X^5 - X^4} \\ 0 \quad \parallel \quad X^2 + 0X + 1 \\ \underline{- X^2 - 0X - 1} \\ 0 \end{array}$$

Find the quotient and remainder using synthetic division.

11. $\frac{x^3 - x^2 - 2x + 6}{x - 2}$

$$\begin{array}{r} 2 | 1 \quad -1 \quad -2 \quad 6 \\ \quad \quad \underline{2} \quad \underline{2} \quad 0 \\ \quad \quad 1 \quad 1 \quad 0 \quad 6 \end{array}$$

(12 and 13) Write the polynomial with specified degree that has the given zeros.

12. degree 3 with zeros -1, 1, 3.

$$(x+1)(x-1)(x-3) = \boxed{x^3 - 3x^2 - x + 3}$$

13. degree 4 with double roots of -2 and 3.

$$(x+2)^2(x-3)^2 = (x^2 + 4x + 4)(x^2 - 6x + 9) = \frac{x^4 - 6x^3 + 9x^2}{x^4 - 2x^3 - 11x^2 + 12x + 36} \quad x^2 - 24x + 36$$

14. List the possible rational zeros of $P(x) = 2x^5 + 3x^3 + 4x^2 - 8$

$$\pm \frac{1, 2, 4, 8}{1, 2} = \boxed{\pm 1, 2, 4, 8, \frac{1}{2}, \frac{3}{2}}$$

Find all the real zeros of the polynomial.

15. $P(x) = x^3 - 3x^2 - 4x + 12$

$$\begin{array}{r} \pm 1, 2, 3, 4, 6, 12 \\ -2 | 1 \quad -3 \quad -4 \quad 12 \\ \quad \underline{-2} \quad \underline{10} \quad \underline{-12} \\ \quad 1 \quad -5 \quad 6 \quad 0 \end{array}$$

$$x^2 - 5x + 6$$

$$(x-3)(x-2)$$

$$x=3, 2, -2$$

16. $P(x) = -x^4 + 10x^2 + 8x - 8$

$$\begin{array}{r} \pm 1, 2, 4, 8 \\ -2 | -1 \quad 0 \quad 10 \quad 8 \quad -8 \\ \quad \underline{-1} \quad \underline{2} \quad \underline{4} \quad \underline{-4} \\ \quad 2 \quad -8 \quad 4 \quad -1 \quad 2 \quad 6 \quad -4 \\ \quad \underline{-1} \quad \underline{4} \quad \underline{-2} \quad \underline{0} \end{array}$$

$$\begin{array}{l} x^3 + 2x^2 + 6x - 4 \\ -x^3 - 10x^2 - 8x \\ \hline 12x^2 + 16x - 4 \\ -12x^2 - 40x \\ \hline 24x - 4 \\ -24x \\ \hline -4 \end{array}$$

17. Use Descartes Rule of Signs to determine how many positive and how many negative real zeros

$P(x) = 2x^4 - 7x^3 + x^2 - 18x + 3$ has.

$$+ - + - +$$

There can be 4, 2, or 0 positive real answers

$$P(-x) = + + + + +$$

There are 0 negative real answers

$$4 \pm \sqrt{16 - 4 \cdot 1 \cdot 2}$$

$$2$$

$$\begin{array}{r} 4 \pm \sqrt{8} = 4 \pm \\ 2 \\ = 2 \pm \sqrt{2} \end{array}$$