

11.1 - 11.4 Parabolas / 1.9 II Circles Review

On 1 - 3 find the equation of the parabola in standard form.

1. focus (1, 0); directrix $x = -3$

$$(h+p, K) \quad x = h-p$$

$$x = \frac{1}{8}y^2 - 1$$

$$K=0$$

$$h+p=1$$

$$-1+p=1$$

$$h-p=-3$$

$$p=+2$$

2. focus (0, -3); vertex (-2, -3)

$$x = \frac{1}{8}(y+3)^2 - 2$$

x changed $p=2, h=-2, K=-3$

3. vertex (5, 1); directrix $y = 4$

$$y = \frac{1}{12}(x-5)^2 + 1$$

$$h$$

$$K=p$$

$$\begin{aligned} 4 &= 1-p \\ 3 &= -p \end{aligned}$$

Find p, the vertex, focus, directrix and focal diameter of each parabola. Graph the parabola.

4. $y^2 + 2y + 8x - 15 = 0$

$$p = -2$$

$$V: (2, -1)$$

$$f: (0, -1)$$

$$d: x = 4$$

$$fd: 8$$

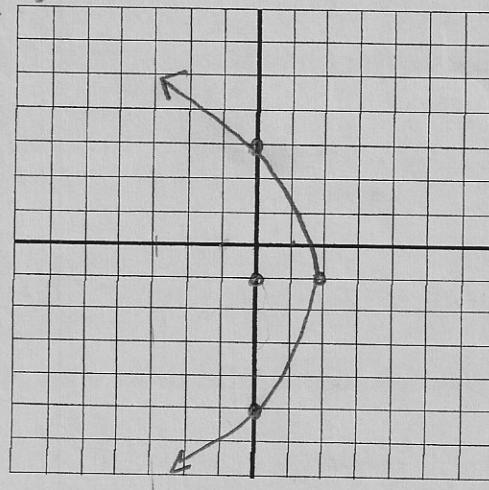
$$(y^2 + 2y + 1) - 15 = -8x +$$

$$(y+1)^2 - 16 = -8x$$

$$\boxed{-\frac{1}{8}(y+1)^2 + 2 = x}$$

$$h=2, K=-1$$

$$p = -2$$



5. $x^2 + 4x - 4y = 12$

$$p = 1$$

$$V: (-2, -4)$$

$$f: (-2, -3)$$

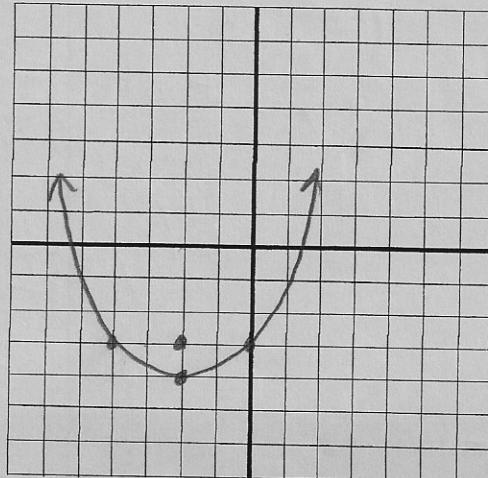
$$d: y = -5$$

$$fd: 4$$

$$(x+2)^2 - 16 = 4y$$

$$\boxed{\frac{1}{4}(x+2)^2 - 4 = y}$$

$$h = -2, K = -4, p = 1$$



6. Find the distance between the points $(1, 3)$ and $(4, 7)$.

$$d = \sqrt{9 + 16} = \sqrt{25} = \boxed{5}$$

7. Find the midpoint of the segment joining the points $(6, -1)$ and $(14, 1)$.

$$\text{mp} \left(\frac{20}{2}, \frac{0}{2} \right) = \boxed{(10, 0)}$$

8. Find the equation of the circle with the center $(-2, 1)$ and radius $4\sqrt{3}$.

$$(x + 2)^2 + (y - 1)^2 = (4\sqrt{3})^2$$

$$\boxed{(x + 2)^2 + (y - 1)^2 = 48}$$

9. Find the center and radius of the circle with the equation $x^2 + y^2 - 10x - 8y = -16$

$$(x^2 - 10x + 25) + (y^2 - 8y + 16) = -16 + 25 + 16$$

$$(x - 5)^2 + (y - 4)^2 = 25 \quad \boxed{C(5, 4) \ r = 5}$$

10. Find the equation of the circle with endpoints of the diameter of $(3, 5)$ and $(-7, -11)$.

$$\text{mp} : \left(-\frac{4}{2}, \frac{-6}{2} \right) = (-2, -3)$$

$$r = \sqrt{25 + 64} = \sqrt{89} = \boxed{\sqrt{89}}$$

$$\boxed{(x + 2)^2 + (y + 3)^2 = 89}$$